

EXTENDED PROCEEDINGS OF

Oxford (CMI and C&S) workshop on IUT theory of Shinichi Mochizuki

December 7-11 2015, L3 Math Institute Univ. Oxford

Letter to participants (I. Fesenko)

Scientific report on the workshop (I. Fesenko)

December 7

9:00-9:20 Ivan Fesenko <i>Foreword</i>	0
9:20-10:10 Shou-Wu Zhang <i>A proof of geometric Szpiro inequality inspired by Bogomolov</i>	1
10:40-11:40 Ulf Kühn <i>Arithmetic of elliptic curves in general position</i>	2
13:30-14:30 Ariyan Javanpeykar <i>Reducing the conjectures to one theorem of IUT</i>	3
15:00-16:00 Yuichiro Hoshi <i>An approximate statement of the main theorem of IUT</i>	4
16:15-17:15 Yuichiro Hoshi <i>Mono-anabelian transport</i>	4
17:20-18:00 <i>Discussions</i>	

December 8

9:00-11:00 <i>Skype session with Shinichi Mochizuki</i>	
11:30-12:30 Fucheng Tan <i>Absolute anabelian geometry</i>	5
13:50-14:50 Fucheng Tan <i>Absolute anabelian geometry</i>	5
15:20-16:20 Jakob Stix <i>Reconstruction of fields using Belyi cuspidalization</i>	6
16:35-17:35 Lars Kuehne <i>Archimedean aspects of absolute anabelian geometry</i>	7
17:35-18:00 <i>Discussions</i>	

December 9

9:00-9:45 Oren Ben-Bassat <i>Frobenioids 1</i>	8
10:00-10:45 Weronika Czerniawska <i>Frobenioids 2</i>	9

11:15-12:15 Tamás Szamuely <i>Geometry and semi-graphs of anabelioids</i>	10
14:10-15:10 Emmanuel Lepage <i>Tempered fundamental group of semi-graphs of anabelioids</i>	11
15:45-16:15 Go Yamashita <i>Motivation from Hodge-Arakelov theory</i>	12
16:30-17:30 Kiran Kedlaya <i>Etale theta function</i>	13
17:30-18:00 <i>Discussions</i>	
December 10	
9:00-10:00 Kiran Kedlaya <i>Etale theta function</i>	13
10:15-11:15 Chung Pang Mok <i>IUT, Introduction to (Hodge) theatres</i>	14
11:45-12:45 Chung Pang Mok <i>IUT, Introduction to (Hodge) theatres</i>	14
13:50-14:50 Chung Pang Mok <i>IUT, Multiradiality of the theta environment</i>	15
15:20-16:20 Yuichiro Hoshi <i>IUT, Hodge-Arakelov-theoretic evaluation</i>	16
16:35-17:35 Yuichiro Hoshi <i>IUT, Hodge-Arakelov-theoretic evaluation</i>	16
17:35-18:00 <i>Discussions</i>	
December 11	
9:00-10:00 Go Yamashita <i>IUT, [IUT-III]</i>	17
10:15-11:15 Go Yamashita <i>IUT, [IUT-III]</i>	17
11:45-12:45 Go Yamashita <i>IUT, [IUT-III]</i>	17
13:40-15:40 <i>Skype session with Shinichi Mochizuki</i>	18
16:10-17:10 Go Yamashita <i>IUT, [IUT-III-IV], with some remarks on the language of species</i>	19
17:10-17:30 Ivan Fesenko <i>Summary and what's next</i>	
0 see this page for survey texts of IUT which you may find useful to read first	
1 this proof can be viewed as an elementary guide or blueprint for IUT, see [B] and also this table ; the key inequality is actually the Milnor-Wood inequality, see e.g. this paper	
2 [NB] and [AE]	

3 Sect. 1-2 of [IUT-IV] without proof of Th 1.10 of [IUT-IV]

4 these follow a very recent [survey of IUT](#) by Yuichiro Hoshi, in Japanese.

One can also recommend three slide talks of the same speaker at a RIMS conference in December 2015 available from section Lectures of [this page](#)

5 [TAAG-I-II]

6 sect.1 of [TAAG-III]

7 sect. 2 and 4 of [TAAG-III]

8 [F], see also [Responses to questions on Frobenioids](#) by Shinichi Mochizuki, in particular Response 8

9 [F], see also [Responses to questions on Frobenioids](#) by Shinichi Mochizuki, in particular Response 8

10 [A]

11 [A] and sect. 2 of [IUT-I]

12 [HAT] and slides 12-23 of [a talk](#) by Go Yamashita at RIMS in March 2015

13 [ET], [picture of covers](#)

14 [IUT-I]

15 sect. 1 of [IUT-II]

16 sect. 2-4 of [IUT-II]

17 [IUT-III]

18 see in particular [Response on a question of Fucheng Tan](#) by Shinichi Mochizuki

19 [IUT-III] and sect. 1 of [IUT-IV], with some remarks on the language of species, sect. 3 of [IUT-IV]

All papers below are authored by Shinichi Mochizuki and available, often with comments, from [this page](#)

[A] [The geometry of anabelioids](#), Publ. Res. Inst. Math. Sci. 40 (2004), 819–881;

[Semi-graphs of anabelioids](#), Publ. Res. Inst. Math. Sci. 42 (2006), 221–322

[AE] [Arithmetic elliptic curves in general position](#), Math. J. Okayama Univ. 52 (2010), 1–28

[B] [Bogomolov's proof of the geometric version of the Szpiro conjecture from the point of view of inter-universal Teichmüller theory](#),
preprint 2015

[ET] [The étale theta function and its frobenioid-theoretic manifestations](#), Publ. Res. Inst. Math. Sci. 45 (2009), 227–349

[F] [The geometry of frobenioids I: The general theory](#), Kyushu J. Math. 62(2008), 293–400;

[The geometry of frobenioids II: Poly-Frobenioids](#), Kyushu J. Math. 62 (2008), 401–460

[HAT] A survey of the Hodge–Arakelov theory of elliptic curves I, in Proc. of Symp. Pure Math. 70, AMS (2002), 533–569;

A survey of the Hodge–Arakelov theory of elliptic curves II, Adv. Stud. Pure Math. 36, Math. Soc. Japan (2002), 81–114

[IUT] Inter-universal Teichmüller theory I: Constructions of Hodge theaters, preprint 2012–2015;

Inter-universal Teichmüller theory II: Hodge-Arakelov-theoretic evaluation, preprint 2012–2015;

Inter-universal Teichmüller theory III: Canonical splittings of the log-theta-lattice, preprint 2012–2015;

Inter-universal Teichmüller theory IV: Log-volume computations and set-theoretic foundations, preprint 2012–2015

[NB] Noncritical Belyi maps, Math. J. Okayama Univ. 46 (2004), 105–113

[TAAG] Topics in absolute anabelian geometry I: Generalities, J. Math. Sci. Univ. Tokyo 19 (2012), 139–242;

Topics in absolute anabelian geometry II: Decomposition groups and endomorphisms, J. Math. Sci. Univ. Tokyo 20 (2013), 171–269;

Topics in absolute anabelian geometry III: Global reconstruction algorithms, J. Math. Sci. Univ. Tokyo 22 (2015), 939–1156